

14.4	Time(s)	Mol A	(a) Mol B	$\Delta$ Mol A	(b) Rate ( $\Delta$ mol A/s)
	0	0.100	0.000		
	40	0.067	0.033	0.033	$8.3 \times 10^{-4}$
	80	0.045	0.055	-0.022	$5.5 \times 10^{-4}$
	120	0.030	0.070	-0.015	$3.8 \times 10^{-4}$
	160	0.020	0.080	-0.010	$2.5 \times 10^{-4}$

(c) The volume of the container must be known to report the rate in units of concentration (mol/L) per time.

14.10 (a)  $\text{rate} = -\Delta[\text{HBr}]/2\Delta t = \Delta[\text{H}_2]/\Delta t = \Delta[\text{Br}_2]/\Delta t$

(b)  $\text{rate} = -\Delta[\text{SO}_2]/2\Delta t = -\Delta[\text{O}_2]/\Delta t = \Delta[\text{SO}_3]/2\Delta t$

(c)  $\text{rate} = -\Delta[\text{NO}]/2\Delta t = -\Delta[\text{H}_2]/2\Delta t = \Delta[\text{N}_2]/\Delta t = \Delta[\text{H}_2\text{O}]/2\Delta t$

14.11 Analyze/Plan. Use Equation 14.4 as needed.

14.12 (a)  $-\Delta[\text{C}_2\text{H}_4]/\Delta t = \Delta[\text{CO}_2]/2\Delta t = \Delta[\text{H}_2\text{O}]/2\Delta t$

$-2\Delta[\text{C}_2\text{H}_4]/\Delta t = \Delta[\text{CO}_2]/\Delta t = \Delta[\text{H}_2\text{O}]/\Delta t$

$\text{C}_2\text{H}_4$  is burning,  $-\Delta[\text{C}_2\text{H}_4]/\Delta t = 0.23 \text{ M/s}$

$\text{CO}_2$  and  $\text{H}_2\text{O}$  are produced, at twice the rate that  $\text{C}_2\text{H}_4$  is consumed.

$\Delta[\text{CO}_2]/\Delta t = \Delta[\text{H}_2\text{O}]/\Delta t = 2(0.23) \text{ M/s} = 0.46 \text{ M/s}$

(b) In this reaction, pressure is a measure of concentration.

$-\Delta[\text{N}_2\text{H}_4]/\Delta t = -\Delta[\text{H}_2]/\Delta t = \Delta[\text{NH}_3]/2\Delta t$

$\text{N}_2\text{H}_4$  is consumed,  $-\Delta[\text{N}_2\text{H}_4]/\Delta t = 45 \text{ torr/hr}$

$\text{H}_2$  is consumed,  $-\Delta[\text{H}_2]/\Delta t = 45 \text{ torr/hr}$

$\text{NH}_3$  is produced at twice the rate that  $\text{N}_2\text{H}_4$  and  $\text{H}_2$  are consumed,

$\Delta[\text{NH}_3]/\Delta t = -2\Delta[\text{N}_2\text{H}_4]/\Delta t = 2(45) \text{ torr/hr} = 90 \text{ torr/hr}$

$\Delta P_T/\Delta t = (+90 \text{ torr/hr} - 45 \text{ torr/hr} - 45 \text{ torr/hr}) = 0 \text{ torr/hr}$

ANSWER

14.15 Analyze/Plan. Follow the logic in Sample Exercise 14.6. Solve:

(a)  $\text{rate} = k[\text{N}_2\text{O}_5] = 4.82 \times 10^{-3} \text{ s}^{-1} [\text{N}_2\text{O}_5]$

(b)  $\text{rate} = 4.82 \times 10^{-3} \text{ s}^{-1} (0.0240 \text{ M}) = 1.16 \times 10^{-4} \text{ M/s}$

(c)  $\text{rate} = 4.82 \times 10^{-3} \text{ s}^{-1} (0.0480 \text{ M}) = 2.31 \times 10^{-4} \text{ M/s}$

When the concentration of  $\text{N}_2\text{O}_5$  doubles, the rate of the reaction doubles.

14.21 Analyze/Plan. Follow the logic in Sample Exercise 14.6. Solve:

(a) From the data given, when  $[\text{OCl}^-]$  doubles, rate doubles. When  $[\text{I}^-]$  doubles, rate doubles. The reaction is first order in both  $[\text{OCl}^-]$  and  $[\text{I}^-]$ .  $\text{rate} = [ \text{OCl}^- ] [\text{I}^- ]$

(b) Using the first set of data:

$$k = \frac{\text{rate}}{[\text{OCl}^-][\text{I}^-]} = \frac{1.36 \times 10^4 \text{ M/s}}{(1.5 \times 10^{-3} \text{ M})(1.5 \times 10^{-3} \text{ M})} = 6.0444 \times 10^3 = 6.04 \times 10^3 \text{ M}^{-1} \text{s}^{-1}$$

(c)  $\text{rate} = \frac{6.044 \times 10^3}{\text{M} \cdot \text{s}} (1.0 \times 10^{-3} \text{ M})(5.0 \times 10^{-4} \text{ M}) = 3.02 \times 10^3 \text{ M/s}$

14.24 (a) Doubling  $[\text{NH}_3]$  while holding  $[\text{BF}_3]$  constant doubles the rate (experiments 1 and 2). Doubling  $[\text{BF}_3]$  while holding  $[\text{NH}_3]$  constant doubles the rate (experiments 4 and 5).

Thus, the reaction is first order in both  $\text{BF}_3$  and  $\text{NH}_3$ ;  $\text{rate} = k[\text{BF}_3][\text{NH}_3]$ .

(b) The reaction is second order overall.

(c) From experiment 1:  $k = \frac{0.2130 \text{ M/s}}{(0.250 \text{ M})(0.250 \text{ M})} = 3.41 \text{ M}^{-1} \text{s}^{-1}$

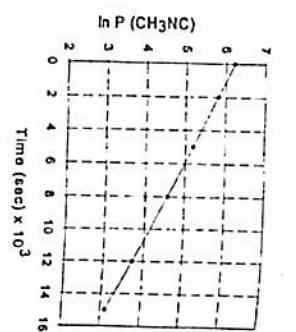
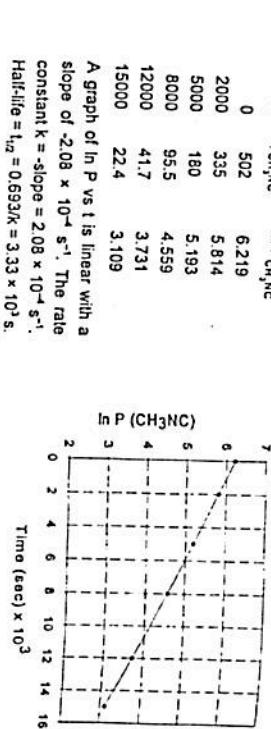
(Any of the five sets of initial concentrations and rates could be used to calculate the rate constant  $k$ . The average of these 5 values is  $k_{avg} = 3.41 \text{ M}^{-1} \text{s}^{-1}$ )

# 23

PS

14.30 (a)  $t_{1/2} = 0.693k = 0.693 \times 7.0 \times 10^{-4} \text{ s}^{-1} = 990 = 9.9 \times 10^2 \text{ s}$

(b)  $k = \frac{0.693}{t_{1/2}} = \frac{0.693}{56.3 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ s}} = 2.052 \times 10^{-4} = 2.05 \times 10^{-4} \text{ s}^{-1}$



14.47 Analyze/Plan. Given  $k_1$  at  $T_1$ , calculate  $k_1$  at  $T_2$ . Change T to Kelvins, then use the Arrhenius equation [14.21] to calculate  $k_2$ . Solve:

$$T_1 = 20^\circ\text{C} + 273 = 293 \text{ K}, \quad T_2 = 60^\circ\text{C} + 273 = 333 \text{ K}; \quad k_1 = 2.75 \times 10^{-2} \text{ s}^{-1}$$

(a)  $\ln \left( \frac{k_1}{k_2} \right) = \frac{E_a}{R} \left( \frac{1}{333} - \frac{1}{293} \right) = \frac{75.5 \times 10^3 \text{ J/mol}}{8.314 \text{ J/mol}} (4.100 \times 10^{-4})$

$$\ln(k_1/k_2) = -3.7229 = -3.72; \quad k_1/k_2 = 0.0242 = 0.024; \quad k_2 = \frac{0.0275 \text{ s}^{-1}}{0.0242} = 1.1 \text{ s}^{-1}$$

(b)  $\ln \left( \frac{k_1}{k_2} \right) = \frac{105 \times 10^3 \text{ J/mol}}{8.314 \text{ J/mol}} \left( \frac{1}{333} - \frac{1}{293} \right) = -5.1776 = -5.18$

$$k_1/k_2 = 5.642 \times 10^{-3} = 5.6 \times 10^{-3}; \quad k_2 = \frac{0.0275 \text{ s}^{-1}}{5.642 \times 10^{-3}} = 4.9 \text{ s}^{-1}$$

14.51 Analyze/Plan. Given a proposed mechanism and an observed rate law, determine which step is rate determining. Solve:

(a) If the first step is slow, the observed rate law is the rate law for this step.  
 $\text{rate} = k[\text{NO}][\text{Cl}_2]$

(b) Since the observed rate law is second-order in  $[\text{NO}]$ , the second step must be slow relative to the first step: the second step is rate determining.

14.73 Analyze/Plan. Let  $k$  = the rate constant for the uncatalyzed reaction;

$$k_c = \text{the rate constant for the catalyzed reaction}$$

According to Equation [14.22],  $\ln k = -E_a/RT + \ln A$

Subtracting  $\ln k$  from  $\ln k_c$ ,

$$\ln k_c - \ln k = \left[ \frac{55 \text{ kJ/mol}}{RT} \cdot \ln A \right] - \left[ \frac{95 \text{ kJ/mol}}{RT} \cdot \ln A \right]. \quad \text{Solve:}$$

(a)  $\ln k_c - \ln k = \left[ \frac{55 \text{ kJ/mol}}{RT} \cdot \ln A \right] - \left[ \frac{95 \text{ kJ/mol}}{RT} \cdot \ln A \right]$ . Solve:  
 $RT = 8.314 \text{ J/K} \cdot \text{mol} \times 298 \text{ K} \times 1 \text{ kJ/1000 J} = 2.478 \text{ kJ/mol}; \quad \ln A \text{ is the same for both reactions.}$

$$\ln (k_c/k) = \frac{95 \text{ kJ/mol} - 55 \text{ kJ/mol}}{2.478 \text{ kJ/mol}}; \quad k_c/k = 1.0 \times 10^7$$

The catalyzed reaction is approximately 10,000,000 (ten million) times faster at 25°C.

(b)  $RT = 8.314 \text{ J/K} \cdot \text{mol} \times 398 \text{ K} \times 1 \text{ kJ/1000 J} = 3.309 \text{ kJ/mol}$

$$\ln (k_c/k) = \frac{40 \text{ kJ/mol}}{3.309 \text{ kJ/mol}}; \quad k_c/k = 1.8 \times 10^4$$

The catalyzed reaction is 180,000 times faster at 125°C.

① To determine rate law, we must 1st determine the rate order for C<sub>4</sub>H<sub>6</sub>. Since no info is given about the [C<sub>3</sub>H<sub>12</sub>] a graph can be helpful.

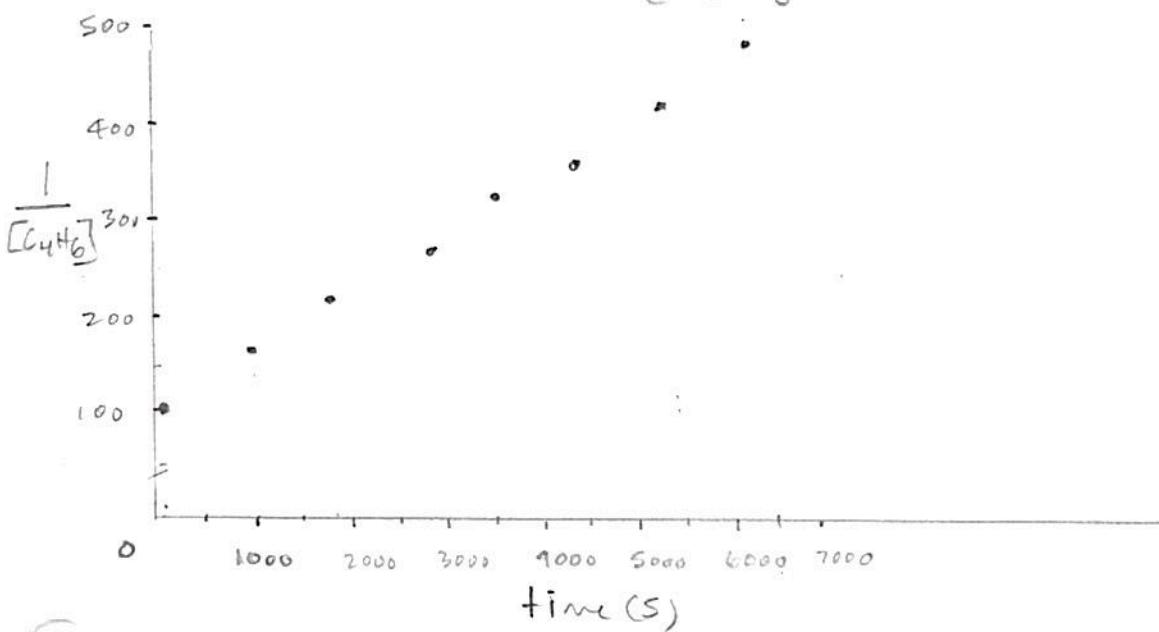
by graphing  $\ln[C_4H_6]_+$  vs. time  
or  $\frac{1}{[C_4H_6]_+}$  vs. time

the rate order can be determined. If the  $\ln[C_4H_6]$  graph yields a straight line, then it is 1st order, if  $\frac{1}{[C_4H_6]}$  is linear then it is second order.

### DATA

Time (s)	[C <sub>4</sub> H <sub>6</sub> ]M	$\ln[C_4H_6]_+$	$\frac{1}{[C_4H_6]_+}$
0	0.01000	-4.61	100
1000	0.00625	-5.08	160
1800	0.00476	-5.35	210
2800	0.00370	-5.60	270
3600	0.00313	-5.77	~320
4400	0.00270	-5.91	370
5200	0.00241	-6.03	415
6200	0.00208	-6.21	480

Since it's easier to graph  $\frac{1}{[C_4H_6]}_+$  vs. t (I will do that)



② As you can see, this is relatively linear, therefore this reaction is second order

$$\text{the rate law is rate} = k[C_4H_6]^2$$

$$\textcircled{B} \quad \frac{\frac{1}{[0.00208]} - \frac{1}{[0.01000]}}{6200\text{s}} = k$$

$$\frac{\frac{1}{0.00208} - \frac{1}{0.01000}}{6200\text{s}}$$

$$\frac{380.77}{6200\text{s} \cdot \text{M}} = \boxed{6.14 \times 10^{-2} \text{ M}^{-1}\text{s}^{-1} = k}$$

From 2nd order rate law  
 $\frac{1}{[A]_t} + \frac{1}{[A]_0} = kt + \frac{1}{[A]_0}$  (14.14)

$$\frac{\frac{1}{[A]_t} - \frac{1}{[A]_0}}{+} = k$$

$$\textcircled{C} \quad \frac{1}{2} \text{ life for } 2\text{nd order rxn} + \frac{1}{2} = \frac{1}{k[A]_0} = \frac{1}{6.14 \times 10^{-2} \text{ M}^{-1}\text{s}^{-1} (0.01\text{M})} = \boxed{1.63 \times 10^3 \text{ seconds}}$$

OR  $\frac{4.52 \times 10^1}{\text{hours}}$   
 OR  $\underline{45 \text{ hours}}$

$\textcircled{2}$  this rxn is doubled as the  $[H_2O_2]$  is doubled, therefore it is first order.

$$\textcircled{A} \quad \text{rate} = k[H_2O_2]$$

$\textcircled{B}$  overall order is first order overall, (one reactant @ 1st order)

$$\textcircled{C} \quad k = \frac{\text{rate}}{[H_2O_2]} \quad \text{I will choose trial 2}$$

$$k = \frac{3.86 \times 10^{-4} \text{ M}}{0.2000 \text{ M} \cdot \text{min.}} = \boxed{1.93 \times 10^{-3} \text{ min}^{-1}}$$

$$\textcircled{D} \quad \frac{1}{2} \text{ life for 1st order rxn} = +\frac{1}{2} = \frac{0.693}{k}$$

$$= \frac{0.693}{1.93 \times 10^{-3} \text{ min}^{-1}} = \boxed{331.1 \text{ minutes}}$$

use this eq

$$\textcircled{E} \quad \ln \frac{[10.0]}{[30.0]} / -k = + = \frac{-1.0906 \text{ min}}{-1.93 \times 10^{-3} \text{ min}^{-1}} = + = \boxed{569 \text{ min.}}$$

$$\ln \frac{[A]_t}{[A]_0} = -kt \quad (14.12)$$



half life ( $t_{\frac{1}{2}}$ ) = 85 seconds.  $[HI]_0 = 0.15 \text{ M}$

$$\text{For 2nd order } t_{\frac{1}{2}} = \frac{1}{k[A_0]} = 85 \text{ sec} = \frac{1}{k(0.15 \text{ M})}$$

Ⓐ  $k = \frac{1}{0.15 \text{ M} (85 \text{ sec})} = [0.0784 \text{ M}^{-1} \text{ sec}^{-1}]$

Ⓑ  $\frac{1}{[A]_t} = k t + \frac{1}{[A]_0}$   $+ = \frac{\frac{1}{[A]_t} - \frac{1}{[A]_0}}{k} = \frac{\frac{1}{0.10 \text{ M}} - \frac{1}{0.30 \text{ M}}}{0.0784 \text{ M}^{-1} \text{ sec}^{-1}}$

$$t = \frac{10 \text{ M}^{-1} - 3.33 \text{ M}^{-1}}{0.0784 \text{ M}^{-1} \text{ sec}^{-1}} = [85.1 \text{ seconds}]$$

④ look @ rxn as beginning @  $t = 0$  w/  $0.0300 \text{ M}$   
and  $t_f = 0.0200 \text{ M}$  @ 200 s.

Ⓐ 1st order  $\ln \frac{[A]_t}{[A]_0} = -kt$   $\ln \frac{[0.02]}{[0.03]} = -kt$   $\frac{-0.4055}{-t} = k = \frac{400}{200} = 2.027 \times 10^{-3} \text{ min}^{-1}$

Ⓑ 1st order  $t_{\frac{1}{2}} = \frac{0.693}{k} = \frac{0.693}{2.027 \times 10^{-3} \text{ min}^{-1}} = [341.9 \text{ min.}]$

Ⓒ  $\ln \frac{[A]_t}{[A]_0} = -kt$  In this case, we want  $[A]_0$ , we'll use  $[A]_t$  at 200 min.

$$\ln \frac{[0.0300]}{[x]} = -2.027 \times 10^{-3} \text{ min}^{-1} (200 \text{ min})$$

$$\ln \frac{0.0300}{x} = -0.4054$$

$$e^{-0.4054} = 0.6667$$

$$\frac{0.0300}{x} = 0.6667 \quad x = 0.04499775 \text{ M}$$

⑤ A)  $[I^-]$  is 1st order because as  $[I^-]$  is cut in half, so is the rate.  
 $[OCl^-]$  is also 1st order because in step (trial 4)  $[I^-]$  is doubled (which would double rxn.) while  $[OCl^-]$  is halved, the rate is halved (stays the same as trial 1),

Therefore  $\boxed{\text{rate} = k[I^-][OCl^-]}$

1st order  
Second order  
Overall  
 $1+1=2$

③  $\frac{\text{rate}}{[I^-][OCl^-]} = k \quad \frac{7.91 \times 10^{-2} \text{ M}}{(0.112 \text{ M})(0.18 \text{ M}) \text{ min}} = \frac{7.91 \times 10^{-2} \text{ M}}{0.0216 \text{ M}^2 \text{ min}}$

rate units are not given (I am assuming  $\frac{\text{M}}{\text{min}}$ ?)

$k = 3.662 \frac{\text{M}}{\text{min}}$

④ initial rate =  $k[I^-][OCl^-]$

$$\text{rate}_0 = \frac{3.662 (0.030 \text{ M})(0.090 \text{ M})}{\text{M min}} = \boxed{9.887 \times 10^{-3} \frac{\text{M}}{\text{min}}}$$